Elevated Achievement Group presents...

Solving the Math Conundrum:
How to Develop Students' Skills
While Expanding Their Metacognition

July 20, 2022



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Presenters

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Session Outcomes

Participants will:

- Examine and utilize instructional strategies that integrate mathematical practices and skills with equal focus, coherence, and rigor for all students.
- Analyze and apply the learning process, examples, and tools for developing metacognition with each mathematical practice.
- Create an action plan that ensures all students receive instruction that fosters their mathematics knowledge and metacognition.

The Math Wars

"The new standards grew out of a long and heated debate about mathematics learning...known as the 'math wars,' pitting conceptual understanding and sense-making against procedures, rules, and memorization. The new math standards grew out of the decades-long attempts to acknowledge that both were important aspects of the math curriculum. By incorporating both..., they brought together both sides of the math wars, building on 'the best of previous state standards plus a large body of evidence from international comparisons and domestic reports and recommendations to define a sturdy staircase to college and career readiness.' (National Governors Association, 2013)"

— The Practices in Action, 2021, page 2

Two Types of Standards

STANDARDS FOR MATHEMATICAL CONTENT	STANDARDS FOR MATHEMATICAL PRACTICE
A list of things students should understand and be able to do by the end of each grade	A list of ways that proficient students engage with mathematics, including thinking skills and habits of mind
Specific mathematical knowledge and skills that follow a step-by-step learning progression across grade levels and courses	 More general processes and proficiencies that evolve over time, influenced by cognitive development and the sophistication of the content
 K-8 organized by grade level; high school organized by conceptual theme 	Standards are the same across all grade levels
Familiar to most teachers	Not as familiar to teachers
Easily and frequently tested, and therefore the focus of the typical math curriculum	 Not as easily or frequently tested, and therefore often neglected in the math curriculum

[—] The Practices in Action, 2021, page 5

Building Math Muscle Memory

"One hallmark of mathematical understanding is the ability to justify, in a way appropriate to the student's mathematical maturity, why a particular mathematical statement is true or where a mathematical rule comes from. There is a world of difference between a student who can summon a mnemonic device to expand a product such as (a + b)(x + y) and a student who can explain where the mnemonic comes from. The student who can explain the rule understands the mathematics and may have a better chance to succeed at a less familiar task such as expanding (a + b)(x + y)."

— The Practices in Action, 2021, page 4

Owning the Mathematical Practices

The Standards

Practice 1

Make sense of problems and persevere in solving them.



Reason abstractly and quantitatively.



Construct viable arguments and critique the reasoning of others.



Model with mathematics.



Use appropriate tools strategically.



Attend to precision.



Look for and make use of structure.



Look for and express regularity in repeated reasoning.

Student Ownership Statements



I can determine what the problem is asking me to do and not give up until I've solved it.



I can make sense of quantities and use math symbols, numbers, or words to represent and solve problems.



I can justify my conclusions with evidence from my work, and I can listen to or read others' arguments and decide if they make sense.



I can use what I know about math symbols, words, pictures, tools, and diagrams to solve everyday problems.



I can determine which tools are the right ones to use when solving problems.



I can communicate precisely what I'm doing and explain my thinking using mathematical language.



I can determine overall structures and patterns to help me solve problems.



I can use what I already know about problem solving strategies, patterns, and other shortcuts to solve problems.

The Standard for Mathematical Practice 1



Make sense of problems and persevere in solving them.

I can determine what the problem is asking me to do and not give up until I've solved it.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

In short, mathematically proficient students:

- Interpret and make meaning of the problem to find a starting point.
- Analyze what is given in order to explain to themselves the meaning of the problem.
- Plan a solution pathway instead of jumping to a solution.
- Monitor their own progress and change the approach if necessary.
- See relationships between various representations.
- Relate current situations to concepts or skills previously learned and connect mathematical ideas to one another.
- Continually ask themselves, "Does this make sense?"
- Can understand various approaches to solutions.



1 Make sense of problems and persevere in solving them.

PRE-K	In Pre–K, students begin to build the understanding that doing mathematics involves solving problems and discussing how they solved them. With prompting and support from adults, students explain the meaning of a problem and look for ways to solve it. Students use concrete objects to help them conceptualize and solve problems. They may check their thinking by asking, "Does this make sense?" or they may try another strategy.
KINDERGARTEN	In Kindergarten, students begin to build the understanding that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Younger students may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" or they may try another strategy.
FIRST GRADE	In first grade, students realize that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Younger students may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They are willing to try other approaches.
SECOND GRADE	In second grade, students realize that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. They may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They make conjectures about the solution and plan out a problem-solving approach.



1 Make sense of problems and persevere in solving them.

THIRD GRADE	In third grade, students know that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Third graders may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They listen to the strategies of others and will try different approaches. They often will use another method to check their answers.
FOURTH GRADE	In fourth grade, students know that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Fourth graders may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They listen to the strategies of others and will try different approaches. They often will use another method to check their answers.
FIFTH GRADE	In fifth grade, students solve problems by applying their understanding of operations with whole numbers, decimals, and fractions including mixed numbers. They solve problems related to volume and measurement conversions. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, "What is the most efficient way to solve the problem?", "Does this make sense?", and "Can I solve the problem in a different way?"
SIXTH GRADE	In grade 6, students solve problems involving ratios and rates and discuss how they solved them. Students solve real world problems through the application of algebraic and geometric concepts. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, "What is the most efficient way to solve the problem?", "Does this make sense?", and "Can I solve the problem in a different way?"



Make sense of problems and persevere in solving them.

SEVENTH GRADE

In grade 7, students solve problems involving ratios and rates and discuss how they solved them. Students solve real world problems through the application of algebraic and geometric concepts. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, "What is the most efficient way to solve the problem?", "Does this make sense?", and "Can I solve the problem in a different way?"

EIGHTH GRADE

In grade 8, students solve real world problems through the application of algebraic and geometric concepts. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, "What is the most efficient way to solve the problem?", "Does this make sense?", and "Can I solve the problem in a different way?"

HIGH SCHOOL

High school students start to examine problems by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. By high school, students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. They check their answers to problems using different methods and continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

— The Practices in Action, 2021, pages 24-25

A Process to Teach the Practice



Make sense of problems and persevere in solving them.

"I can determine what the problem is asking me to do and not give up until I've solved it."

Process

Process to make sense of problems

- Read the problem out loud.
- 2. Identify and clarify each word that tells you what to do mathematically.
- 3. Explain the problem in your own words.
- 4. Explain how you will know you have solved the problem correctly.

Process to persevere in solving them

- Make a plan for solving the problem.
- Begin to solve the problem.
- 3. Each time you get stuck, identify where you got stuck.
- 4. Ask for help, as needed.
- 5. Keep working until you've solved the problem correctly.

A Reflection Guide for the Practice



Make sense of problems and persevere in solving them.

"I can determine what the problem is asking me to do and not give up until I've solved it."

To what degree can you determine what the problem is asking you to do and not give up until you've solved it?

sometimes always never

- What does "make sense of problems" mean?
- What does "persevere in solving them" mean?
- How do you determine what the problem is asking you to do?
- How do you not give up until you've solved the problem?
- How does "making sense of problems and persevering in solving them" help you?

From Process to Practice to Metacognition



Make sense of problems and persevere in solving them.

The Practice in Action: When presented with a problem that asks students to analyze proportional relationships and use them to solve real-world and mathematical problems, seventh graders utilizing this practice use their understanding of ratios to discuss how they solved the problem.

The ratio of time that Leo spends on math homework to science homework is 5 to 4. If he spends 40 minutes on math homework, how much time does Leo spend on science homework?

TEACHER: What is the problem asking you to do?

STUDENT: The problem is asking me to find out how much time Leo spends on science homework.

TEACHER: What is your plan to solve the problem?

STUDENT: I can solve this problem by using my understanding that a ratio compares two numbers. This problem gives me the ratio of time spent on math and science homework and the exact amount for math. I can take that information to set up the ratios in fraction form and efficiently cross multiply to find the amount of time for the science homework.

TEACHER: Does this make sense?

STUDENT: Yes, because I planned my solution pathway instead of jumping to the solution. This helps me make sure I don't miss a critical piece of information in the problem.

TEACHER: How did making sense of the problem and persevering in solving it help you?

STUDENT: It helped me to understand what the problem is really asking me to do. Then, I could figure out how to solve it and then work on it until it was finished.

Tools for Developing Mathematical Thinkers and Speakers



Make sense of problems and persevere in solving them.

Questions to Foster Metacognition

What is the problem asking you to do?

What is your plan for solving the problem?

How would you explain the problem in your own words?

How could you go about solving the problem?

Are there any other ways you could approach the problem?

How does looking for the most efficient way to solve the problem help you?

What are some other strategies you might try?

Does this make sense? What can you do if you are struggling?

Why is it important to be able to identify when you are struggling?

How do you know when you have solved the problem?

Why does explaining the problem in your own words help you?

How does making sense of problems and persevering in solving them help you?

Tools for Developing Mathematical Thinkers and Speakers



Make sense of problems and persevere in solving them.

Ownership Statements Being able to explain the problem is important because _____. Planning a solution pathway instead of jumping to a solution is important because _____. I can solve the problem by _____. Another way to solve this problem is _____. Looking for efficient ways to represent and solve the problem helps me because _____. Understanding that there might be other ways to find the solution helps me because _____.

important because _____.

helps me because _____.

The Standard for Mathematical Practice 6



Attend to precision.

I can communicate precisely what I'm doing and explain my thinking using mathematical language.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

In short, mathematically proficient students:

- Communicate precisely with others and try to use clear mathematical language when discussing their reasoning.
- Understand the meanings of symbols used in mathematics and can label quantities appropriately.
- Express numerical answers with a degree of precision appropriate for the problem context.
- Calculate efficiently and accurately.

— The Practices in Action, 2021, pages 52–53



Attend to precision.

PRE-K	As pre-k students begin to develop their mathematical communication skills, teachers model clear and precise language and encourage students to try and use it in their discussions with others and in their own reasoning.
KINDERGARTEN	As kindergarteners begin to develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning.
FIRST GRADE	As young children begin to develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and when they explain their own reasoning.
SECOND GRADE	As children begin to develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and when they explain their own reasoning.
THIRD GRADE	As third graders develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, when figuring out the area of a rectangle they record their answers in square units.
FOURTH GRADE	As fourth graders develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, they use appropriate labels when creating a line plot.
FIFTH GRADE	Students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students use appropriate terminology when referring to expressions, fractions, geometric figures, and coordinate grids. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, when figuring out the volume of a rectangular prism they record their answers in cubic units.



Attend to precision.

SIXTH GRADE	In grade 6, students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students use appropriate terminology when referring to rates, ratios, geometric figures, data displays, and components of expressions, equations or inequalities.
SEVENTH GRADE	In grade 7, students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students define variables, specify units of measure, and label axes accurately. Students use appropriate terminology when referring to rates, ratios, probability models, geometric figures, data displays, and components of expressions, equations or inequalities.
EIGHTH GRADE	In grade 8, students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students use appropriate terminology when referring to the number system, functions, geometric figures, and data displays.
HIGH SCHOOL	High school students try to communicate precisely to others by using clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

— The Practices in Action, 2021, pages 54-55

A Process to Teach the Practice



Attend to precision.

"I can communicate precisely what I'm doing and explain my thinking using mathematical language."

Process to attend to precision

- Explain the problem using specific mathematical language for words and symbols.
- Explain the problem using specific units of measure.
- 3. Explain how you will solve the problem using specific mathematical language and units of measure.
- As you are solving the problem, explain what you are doing using specific mathematical language and units of measure.
- Explain your thinking in both writing and speaking.

- The Practices in Action, 2021, page 56

A Reflection Guide for the Practice



Attend to precision.

"I can communicate precisely what I'm doing and explain my thinking using mathematical language."

Reflection

To what degree can you communicate precisely what you are doing and explain your thinking using mathematical language?

> 5 sometimes always never

What does "attend to precision" mean?

How do you communicate precisely what you are doing and explain your thinking using mathematical language?

How does attending to precision help you?

From Process to Practice to Metacognition



Attend to Precision.

The Practice in Action: When presented with solving systems of equations in a problem, Algebra I students utilizing this practice graph the equations to verify the solution of the system.

Solve the following system of equations using substitution and graph the equations:

$$6x - 5y = 34$$

 $3x + 2y = 8$

TEACHER: What is the problem asking you to do?

STUDENT: The problem is asking me to solve a system of equations using substitution and then to graph the equations.

TEACHER: What mathematical terms apply in this situation?

STUDENT: The terms that apply are "system of equations" and "substitution."

TEACHER: What symbols or mathematical notations are important in this problem?

STUDENT: The positive and negative numbers are important because I have to pay attention to them when solving correctly.

TEACHER: How will you solve the system of equations and graph each equation?

STUDENT: I start by rearranging the second equation to isolate the y variable: y equals 4 minus 1.5 times x. Then I substitute the expression 4 minus 1.5 times x for y in the first equation and solve for x. I need to check to make sure the solution I get makes both equations in the system true. If my answer is yes, I can graph the equations to verify the solution of the system. If my answer is no, then I need to check my work.

TEACHER: How could you test your solution?

STUDENT: I could substitute the values for x or for y into the original equations to determine if the result is true. If it is, my original answer is correct.

TEACHER: How does attending to precision help you?

STUDENT: It helps me be clear about the mathematical symbols and language needed to solve the problem.

Tools for Developing Mathematical Thinkers and Speakers



Attend to precision.

Questions to Foster Metacognition

What is the problem asking you to do?

What mathematical terms apply in this situation?

How you might show that your solution answers this problem?

How could you test your solution to see if it answers the problem?

Is there a more efficient strategy for solving the problem?

How are you showing the meaning of the quantities?

What symbols or mathematical notations are important in this problem?

What mathematical language, definitions, or properties can you use to explain ______

How does being able to communicate precisely with others help you?

Why is using clear mathematical language when discussing your reasoning important?

How does understanding the meaning of symbols used in mathematics help you?

Why is being able to label quantities appropriately important?

Why is being able to express numerical answers with a degree of precision appropriate for the problem context important?

Why is being able to calculate efficiently and accurately important?

How does attending to precision help you solve the problem?

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Tools for Developing Mathematical Thinkers and Speakers



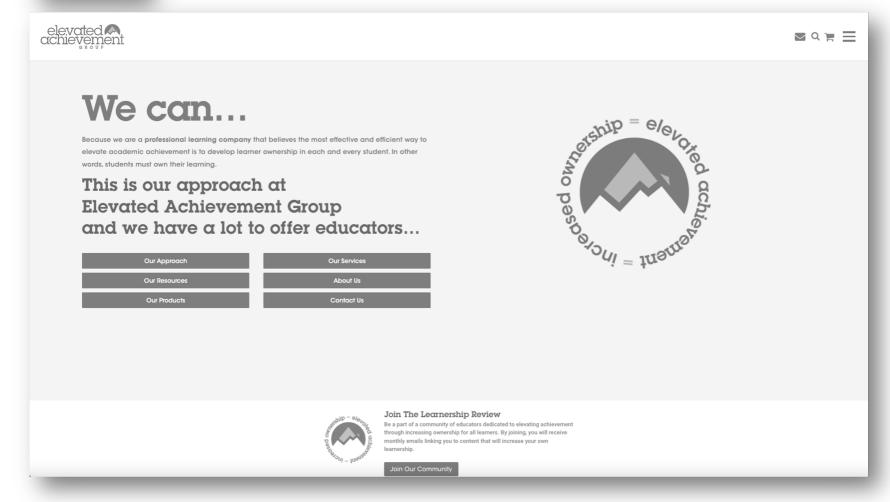
Attend to precision.

Ownership Statements		
Being able to communicate precisely with others helps me because		
Using clear mathematical language when discussing my reasoning is important because		
Understanding the meaning of symbols used in mathematics helps me because		
Being able to label quantities appropriately is important because		
Being able to express numerical answers with a degree of precision appropriate for the problem context is important because		
Being able to calculate efficiently and accurately is important because		
Attending to precision helps me		

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Why does Elevated Achievement Group exist?

We exist because we believe that in order for each and every learner to achieve at higher levels they must own their learning.

- We believe that we can support you in developing learner ownership and elevating achievement—of students, teachers, and administrators.
- We provide professional learning experiences that...
 - Promote a growth mindset.
 - Actively engage you in the learning rather than just participating.
 - Exemplify respect, cooperation, collaboration, and risk-taking
 - Ensure that developing ownership is at the center of all decision-making.
- We believe that increased ownership leads to elevated achievement to such a degree that we put it in our name. We want to be part of a professional group of educators that elevates student achievement—for each and every student—at your school or district.

Your kids are our kids. Your success is our success.

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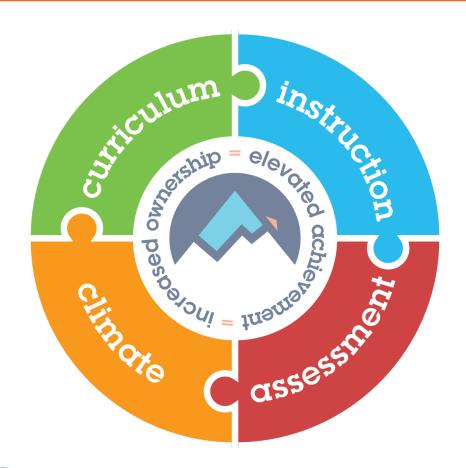
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